











## Expected Running Time, Part 2



- Probabilistic Fact #1: The expected number of coin tosses required in order to get one head is two
- Probabilistic Fact #2: Expectation is a linear function:
  - E(X+Y) = E(X) + E(Y)
  - E(cX) = cE(X)
- Let T(n) denote the expected running time of quick-select.
- By Fact #2,
  - $T(n) \le T(3n/4) + bn*$ (expected # of calls before a good call)
- By Fact #1,
  - $T(n) \le T(3n/4) + 2bn$
- That is, T(n) is a geometric series:
- $T(n) \le 2bn + 2b(3/4)n + 2b(3/4)^2n + 2b(3/4)^3n + \dots$
- So T(n) is O(n).
- We can solve the selection problem in O(n) expected time.

election

