

Priority Queue ADT (§7.1)

- A priority queue stores a collection of items
- An item is a pair (key, element)
- Main methods of the Priority Queue ADT
 - insertItem(k, o) inserts an item with key k and element o
 - removeMin() removes the item with the smallest key



- minKey(k, o) returns, but does not remove, the smallest key of an item
- minElement() returns, but does not remove, the element of an item with smallest key
- size(), isEmpty() Applications:
 - Standby flyers
 - Auctions

 - Stock market

Heaps and Priority Queues

Total Order Relation



- queue can be arbitrary objects on which an order is defined
- Two distinct items in a priority queue can have the same key
- Keys in a priority
 Mathematical concept of total order relation ≤
 - Reflexive property:
 - Antisymmetric property: $x \le y \land y \le x \Rightarrow x = y$
 - Transitive property: $x \le y \land y \le z \Rightarrow x \le z$

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Comparator ADT (§7.1.4)



- A comparator encapsulates the action of comparing two objects according to a given total order
- A generic priority queue uses a comparator as a template argument, to define the comparison function (<,=,>)
- The comparator is external to the keys being compared. Thus, the same objects can be sorted in different ways by using different comparators.
- When the priority queue needs to compare two keys, it uses its comparator

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Using Comparators in C++



- A comparator class overloads the "()" operator with a comparison function.
- Example: Compare two points in the plane lexicographically.

class LexCompare { public:

int operator()(Point a, Point b) { if (a.x < b.x) return -1 else if (a.x > b.x) return +1 else if (a.y < b.y) return -1 else if (a.y > b.y) return +1 else return 0;

- To use the comparator, define an object of this type, and invoke it using its "()" operator:
- Example of usage:

Point p(2.3, 4.5); Point q(1.7, 7.3); LexCompare lexCompare;

if (lexCompare(p, q) < 0) cout << "p less than q"; else if (lexCompare(p, q) == 0) cout << "p equals q"; else if (lexCompare(p, q) > 0) cout << "p greater than q";

Heaps and Priority Queues

Sorting with a Priority Queue (§7.1.2)



- We can use a priority queue to sort a set of comparable elements
 - Insert the elements one by one with a series of insertItem(e, e) operations
 - Remove the elements in sorted order with a series of removeMin() operations
- The running time of this sorting method depends on the priority queue implementation

Algorithm PO-Sort(S. C)

Input sequence S, comparator C for the elements of S**Output** sequence S sorted in increasing order according to C $P \leftarrow$ priority queue with comparator C

while !S.isEmpty ()

 $e \leftarrow S.remove(S. first())$ P.insertItem(e, e)

while !P.isEmpty() $e \leftarrow P.minElement()$ P.removeMin() S.insertLast(e)

Heaps and Priority Queues







































